# Package: ERPM (via r-universe)

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Title Exponential Random Partition Models Version 0.2.0.9000 Date 2024-05-03 **Description** Simulates and estimates the Exponential Random Partition Model presented in the paper Hoffman, Block, and Snijders (2023) <doi:10.1177/00811750221145166>. It can also be used to estimate longitudinal partitions, following the model proposed in Hoffman and Chabot (2023) <doi:10.1016/j.socnet.2023.04.002>. The model is an exponential family distribution on the space of partitions (sets of non-overlapping groups) and is called in reference to the Exponential Random Graph Models (ERGM) for networks. License GPL (>= 3)**Depends** R (>= 4.2)Imports numbers, utils, stats, igraph, RColorBrewer, snowfall **Suggests** knitr, rmarkdown, testthat (>= 3.0.0) Config/testthat/edition 3 **Encoding UTF-8** LazyData true **Roxygen** list(markdown = TRUE) RoxygenNote 7.3.1 Collate 'erpm-package.R' 'functions\_utility.R' 'functions\_Metropolis.R' 'functions\_burninthining.R' 'functions\_change\_statistics.R' 'functions\_estimate.R' 'functions\_exactcalculations.R' 'functions\_exchange\_algorithm.R' 'functions\_loglikelihood.R' 'functions\_output.R' 'functions\_phase1.R' 'functions\_phase2.R' 'functions\_phase3.R' 'functions\_statistics.R' 'functions\_visualisation.R' 'outcomeObjects.R' URL https://github.com/stocnet/ERPM

Type Package

2 Contents

BugReports	https://github.com/stocnet/ERPM/issues
Repository	https://stocnet.r-universe.dev
RemoteUrl	https://github.com/stocnet/erpm
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# **Contents**

Bell_constraints
calculate_denominator_Dirichlet_restricted
calculate_proba_Dirichlet_restricted
check_sizes
computeStatistics
computeStatistics_multiple
compute_averagesize
compute_numgroups_denominator
correlation_between
correlation_within
correlation_with_size
count_classes
CUP
draw_Metropolis_multiple
draw_Metropolis_single
estimate_ERPM
estimate_logL
estimate_multipleERPM
exactestimates_numgroups
find_all_partitions
gridsearch_burninthining_multiple
gridsearch_burninthining_single
gridsearch_burnin_single
gridsearch_thining_single
group_size
icc
number_categories
number_ties
order_groupids
outcomeObjects
phase1
plot_averagesizes
plot_numgroups_likelihood
plot_partition
print.results.bayesian.erpm
print.results.list.erpm
print.results.p3.erpm
proportion isolate

Bell\_constraints 3

	range_attribute																			. 41	
	run_phase1_multiple	e																		. 41	
	run_phase1_single																			. 43	
	run_phase2_multiple																				
	run_phase2_single																				
	run_phase3_multiple																				
	run_phase3_single																				
	same_pairs																				
	similar_pairs																				
	simulate_burninthin																				
	simulate_burninthin																				
	simulate_burnin_sin																				
	simulate_thining_sin	_																			
	Stirling2_constraints																				
	8 = 11 11 11																				
Index																				60	
Bell	constraints	Function to	calcı	ılate	e th	e n	um	hei	r ot	f n	arti	tio	ns	wit	h o	roi	ıns	of	siz	es	
		between smi							<i>-</i> J	P				.,.,	- 8		·PS	J	~~~	,	
		222011 3		~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~																	

# Description

Function to calculate the number of partitions with groups of sizes between smin and smax

# Usage

```
Bell_constraints(n, smin, smax)
```

# Arguments

n number of nodes
smin minimum group size possible in the partition
smax minimum group size possible in the partition

#### Value

a numeric

```
n <- 6
size_min <- 2
size_max <- 4
Bell_constraints(n,size_min,size_max)</pre>
```

calculate\_denominator\_Dirichlet\_restricted

Calculate Dirichlet denominator

## **Description**

Recursive function to calculate the denominator for the model with a single statistic for the number of groups and a given parameter value. The set of possible partitions can be restricted to partitions with groups of a certain size.

## Usage

calculate\_denominator\_Dirichlet\_restricted(n, smin, smax, alpha, results)

## **Arguments**

n	number	of	nodes

smin minimum size for a group smax maximum size for a group

alpha parameter value

results a list

## Value

a numeric

## **Description**

Calculate the probability of observing a partition with a given number of groups for a model with a single statistic for the number of groups and a given parameter value. The set of possible partitions can be restricted to partitions with groups of a certain size.

#### Usage

```
calculate_proba_Dirichlet_restricted(alpha, stat, n, smin, smax)
```

check\_sizes 5

## **Arguments**

alpha parameter value

stat observed stat (number of groups)

n number of nodes

smin minimum size for a group
smax maximum size for a group

#### Value

a numeric

check\_sizes

Function to determine whether a partition contains the allowed group

sizes

# Description

Function to determine whether a partition contains the allowed group sizes

## Usage

```
check_sizes(partition, sizes.allowed, numgroups.allowed)
```

# Arguments

partition observed partition

sizes.allowed vector containing possible group sizes in the partition

numgroups.allowed

vector containing possible number of groups in the partition

#### Value

boolean

computeStatistics

Compute Statistics

## **Description**

Function that computes the statistic vector for a given partition and a given model

## Usage

```
computeStatistics(partition, nodes, effects, objects)
```

## **Arguments**

partition vector, A partition nodes data frame, Node set

effects list with a vector "names", and a vector "objects", Effects/sufficient statistics list with a vector "name", and a vector "object", Objects used for statistics calobjects

culation

#### Value

the statistics

```
computeStatistics_multiple
```

Compute Statistics multiple

## **Description**

Function that computes the statistic vector for given (multiple) partitions and a given model

# Usage

```
computeStatistics_multiple(
  partitions,
  presence.tables,
 nodes,
  effects,
 objects,
  single.obs = NULL
)
```

compute\_averagesize 7

#### **Arguments**

partitions Observed partitions

presence.tables

to indicate which nodes were present when

nodes Node set (data frame)

effects Effects/sufficient statistics (list with a vector "names", and a vector "objects")

"object")

single.obs equal NULL by default

#### Value

A list

compute\_averagesize

Compute the average size of a random partition

# Description

Recursive function to compute the average size of a random partition for a given number of nodes

## Usage

```
compute_averagesize(num.nodes)
```

# Arguments

num.nodes

number of nodes

#### Value

a numeric

```
n <- 6
compute_averagesize(n)</pre>
```

8 correlation\_between

```
compute_numgroups_denominator
```

Compute denominator for model with number of groups

# Description

Recursive function to compute the value of the denominator for the model with a single statistic which is the number of groups

## Usage

```
compute_numgroups_denominator(num.nodes, alpha)
```

## **Arguments**

num.nodes number of nodes alpha parameter value

#### Value

a numeric

correlation\_between

Between groups correlation

#### **Description**

This function computes the correlation between the group averages of the two attributes.

# Usage

```
correlation_between(partition, attribute1, attribute2)
```

## **Arguments**

partition A partition (vector)

attribute1 A vector containing the values of the first attribute
attribute2 A vector containing the values of the second attribute

#### Value

A number corresponding to the correlation coefficient

correlation\_within 9

## **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(3,5,23,2,1,0,3,9,2)
at2 <- c(3,5,20,2,1,0,0,9,0)
correlation_between(p,at,at2)</pre>
```

correlation\_within

Within groups correlation

# Description

This function computes the correlation between the two attributes for individuals in the same group.

## Usage

```
correlation_within(partition, attribute1, attribute2, group)
```

# Arguments

partition	A partition (vector)
attribute1	A vector containing the values of the first attribute
attribute2	A vector containing the values of the second attribute
group	A number indicating the selected group

#### Value

A number corresponding to the correlation coefficient

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(3,5,23,2,1,0,3,9,2)
at2 <- c(3,5,20,2,1,0,0,9,0)
correlation_within(p,at,at2,4)</pre>
```

10 count\_classes

correlation\_with\_size Correlation with size

#### Description

This function computes the correlation between an attribute and the size of the groups.

## Usage

```
correlation_with_size(partition, attribute, categorical)
```

#### **Arguments**

partition A partition (vector)

attribute A vector containing the values of the attribute

categorical A Boolean (True or False) indicating if the attribute is categorical

#### Value

A number corresponding to the correlation coefficient if the attribute is numerical or the correlation ratio if the attribute is categorical.

#### **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(3,5,23,2,1,0,3,9,2)
correlation_with_size(p,at,categorical=FALSE)</pre>
```

count\_classes

Function to count the number of partitions with a certain group size structure, for all possible group size structure. Function to use after calling the "find\_all\_partitions" function.

## **Description**

Function to count the number of partitions with a certain group size structure, for all possible group size structure. Function to use after calling the "find\_all\_partitions" function.

#### Usage

```
count_classes(allpartitions)
```

# **Arguments**

allpartitions matrix containing all possible partitions for a nodeset

CUP 11

#### Value

integer(number of partitions with different group structures)

#### **Examples**

```
#find partitions first
n <- 6
all_partitions <- find_all_partitions(n)
# count classes
counts_partition_classes <- count_classes(all_partitions)</pre>
```

CUP

CUP

## Description

This function tests a partition statistic against a "conditional uniform partition null hypothesi: It compares a statistic computed on an observed partition and the same statistic computed on a set of permuted partition (partitions with the same group structure as the observed partition, with nodes being permuted).

#### Usage

```
CUP(observation, fun, permutations = NULL, num.permutations = 1000)
```

## Arguments

observation A vector giving the observed partition

fun A function used to compute a given partition statistic to be computed

permutations A matrix, whose lines contain partitions which are permutations of the observed

partition. This argument is NULL by default (in that case, the permutations are

created automatically).

num.permutations

An integer indicating the number of permutations to generate, if they are not

already given. 1000 permutations are generated by default.

#### **Details**

This test is similar to Conditional Uniform Graph tests in networks (we translate this into Condtional Uniform Partition tests).

#### Value

The value of the statistic calculated for the observed partition, the mean value of the statistic among permuted partitions, the standard deviation of the statistic among permuted partitions, the proportion of permutation below the observed statistic, the proportion of permutation above the observed statistic, the lower boundary of the 95% CI, the upper boundary of the 95% CI

#### **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(0,1,1,1,1,0,0,0,0)
CUP(p,fun=function(x){same_pairs(x,at,'avg_pergroup')})</pre>
```

draw\_Metropolis\_multiple

Draw Metropolis multiple

#### **Description**

Function to sample the model with a Markov chain (single partition procedure).

#### Usage

```
draw_Metropolis_multiple(
  theta,
  first.partitions,
 presence.tables,
 nodes,
 effects,
  objects,
 burnin,
  thining,
  num.steps,
  neighborhood = c(0.7, 0.3, 0),
 numgroups.allowed,
 numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  return.all.partitions = FALSE,
  verbose = FALSE
)
```

## **Arguments**

```
theta model parameters

first.partitions
    starting partition for the Markov chain

presence.tables
    matrix indicating which actors were present for each observations (mandatory)

nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects objects used for statistics calculation (list with a vector "name", and a vector "object")
```

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

num.steps number of samples

neighborhood = c(0.7,0.3,0), way of choosing partitions: probability vector (2 actors swap,

merge/division, single actor move, single pair move, 2 pairs swap, 2 groups

reshuffle)

numgroups.allowed

= NULL, # vector containing the number of groups allowed in the partition (now, it only works with vectors like num min:num max)

numgroups.simulated

= NULL, # vector containing the number of groups simulated

sizes.allowed = NULL, vector of group sizes allowed in sampling (now, it only works for

vectors like size\_min:size\_max)

sizes.simulated

= NULL, vector of group sizes allowed in the Markov chain but not necessraily sampled (now, it only works for vectors like size\_min:size\_max)

return.all.partitions

= FALSE, option to return the sampled partitions on top of their statistics (for

verbose

logical: should intermediate results during the estimation be printed or not? Defaults to FALSE.

#### Value

A list

```
# define an arbitrary set of n = 6 nodes with attributes, and an arbitrary covariate matrix
nodes <- data.frame(label = c("A", "B", "C", "D", "E", "F"),</pre>
                     gender = c(1,1,2,1,2,2),
                     age = c(20, 22, 25, 30, 30, 31))
friendship <- matrix(c(0, 1, 1, 1, 0, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 0, 0,
                        0, 1, 1, 0, 0, 1,
                        0, 0, 0, 0, 1, 0), 6, 6, TRUE)
# specify whether nodes are present at different points of time
presence.tables \leftarrow matrix(c(1, 1, 1, 1, 1, 1,
                             0, 1, 1, 1, 1, 1,
                             1, 0, 1, 1, 1, 1), 6, 3)
# choose effects to be included in the estimated model
effects_multiple <- list(names = c("num_groups","same","diff","tie","inertia_1"),</pre>
                 objects = c("partitions", "gender", "age", "friendship", "partitions"),
```

```
objects2 = c("","","","",""))
objects_multiple <- list()</pre>
objects_multiple[[1]] <- list(name = "friendship", object = friendship)</pre>
# set parameter values for each of these effects
parameters <- c(-0.2,0.2,-0.1,0.5,1)
# set a starting point for the simulation
first.partitions <- matrix(c(1, 1, 2, 2, 2, 3,
                             NA, 1, 1, 2, 2, 2,
                              1, NA, 2, 3, 3, 1), 6, 3)
# generate the simulated sample
nsteps <- 50
sample <- draw_Metropolis_multiple(theta = parameters,</pre>
                                    first.partitions = first.partitions,
                                    nodes = nodes,
                                    presence.tables = presence.tables,
                                    effects = effects_multiple,
                                    objects = objects_multiple,
                                    burnin = 100,
                                    thining = 100,
                                    num.steps = nsteps,
                                    neighborhood = c(0,1,0),
                                    numgroups.allowed = 1:n,
                                    numgroups.simulated = 1:n,
                                    sizes.allowed = 1:n,
                                    sizes.simulated = 1:n,
                                    return.all.partitions = TRUE)
```

draw\_Metropolis\_single

Draw Metropolis single

#### **Description**

Function to sample the model with a Markov chain (single partition procedure).

#### Usage

```
draw_Metropolis_single(
  theta,
  first.partition,
  nodes,
  effects,
  objects,
```

```
burnin,
thining,
num.steps,
neighborhood = c(0.7, 0.3, 0),
numgroups.allowed = NULL,
numgroups.simulated = NULL,
sizes.allowed = NULL,
sizes.simulated = NULL,
return.all.partitions = FALSE
)
```

#### **Arguments**

theta model parameters

first.partition

starting partition for the Markov chain

nodes nodeset (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects used for statistics calculation (list with a vector "name", and a vector

"object")

burnin integer for the number of burn-in steps before sampling

thining integer for the number of thining steps between sampling

num.steps number of samples

neighborhood = c(0.7,0.3,0), way of choosing partitions: probability vector (2 actors swap,

merge/division, single actor move, single pair move, 2 pairs swap, 2 groups

reshuffle)

numgroups.allowed

= NULL, # vector containing the number of groups allowed in the partition (now,

it only works with vectors like num\_min:num\_max)

numgroups.simulated

= NULL, # vector containing the number of groups simulated

sizes.allowed = NULL, vector of group sizes allowed in sampling (now, it only works for

vectors like size\_min:size\_max)

sizes.simulated

= NULL, vector of group sizes allowed in the Markov chain but not necessraily

sampled (now, it only works for vectors like size\_min:size\_max)

return.all.partitions

= FALSE option to return the sampled partitions on top of their statistics (for

GOF)

#### Value

A list

```
# define an arbitrary set of n = 6 nodes with attributes, and an arbitrary covariate matrix
nodes <- data.frame(label = c("A","B","C","D","E","F"),</pre>
                    gender = c(1,1,2,1,2,2),
                     age = c(20, 22, 25, 30, 30, 31)
friendship \leftarrow matrix(c(0, 1, 1, 1, 0, 0,
                       1, 0, 0, 0, 1, 0,
                       1, 0, 0, 0, 1, 0,
                       1, 0, 0, 0, 0, 0,
                        0, 1, 1, 0, 0, 1,
                        0, 0, 0, 0, 1, 0), 6, 6, TRUE)
# choose the effects to be included (see manual for all effect names)
effects <- list(names = c("num_groups", "same", "diff", "tie"),</pre>
objects = c("partition", "gender", "age", "friendship"))
objects <- list()</pre>
objects[[1]] <- list(name = "friendship", object = friendship)</pre>
# set parameter values for each of these effects
parameters <-c(-0.2, 0.2, -0.1, 0.5)
# generate simulated sample, by setting the desired additional parameters for the
# Metropolis sampler and choosing a starting point for the chain (first.partition)
nsteps <- 100
sample <- draw_Metropolis_single(theta = parameters,</pre>
                                  first.partition = c(1,1,2,2,3,3),
                                  nodes = nodes.
                                  effects = effects,
                                  objects = objects,
                                  burnin = 100,
                                  thining = 10,
                                  num.steps = nsteps,
                                  neighborhood = c(0,1,0),
                                  numgroups.allowed = 1:n,
                                  numgroups.simulated = 1:n,
                                  sizes.allowed = 1:n,
                                  sizes.simulated = 1:n,
                                  return.all.partitions = TRUE)
# or: simulate an estimated model
partition <- c(1,1,2,2,2,3) # the partition already defined for the (previous) estimation
nsimulations <- 1000
simulations <- draw_Metropolis_single(theta = estimation$results$est,</pre>
                                       first.partition = partition,
                                       nodes = nodes,
                                       effects = effects,
                                       objects = objects,
                                       burnin = 100,
                                       thining = 20,
```

estimate\_ERPM 17

```
num.steps = nsimulations,
neighborhood = c(0,1,0),
sizes.allowed = 1:n,
sizes.simulated = 1:n,
return.all.partitions = TRUE)
```

estimate\_ERPM

Estimate ERPM

## **Description**

Function to estimate a given model for a given observed partition. All options of the algorithm can be specified here.

#### Usage

```
estimate_ERPM(
  partition,
  nodes,
  objects,
  effects,
  startingestimates,
  gainfactor = 0.1,
  a.scaling = 0.8,
  r.truncation.p1 = -1,
  r.truncation.p2 = -1,
  burnin = 30,
  thining = 10,
  length.p1 = 100,
 min.iter.p2 = NULL,
 max.iter.p2 = NULL,
 multiplication.iter.p2 = 100,
  num.steps.p2 = 6,
  length.p3 = 1000,
  neighborhood = c(0.7, 0.3, 0),
  fixed.estimates = NULL,
  numgroups.allowed = NULL,
  numgroups.simulated = NULL,
  sizes.allowed = NULL,
  sizes.simulated = NULL,
  double.averaging = FALSE,
  inv.zcov = NULL,
  inv.scaling = NULL,
  parallel = FALSE,
  parallel2 = FALSE,
  cpus = 1,
```

18 estimate\_ERPM

```
verbose = FALSE
)
```

## **Arguments**

partition observed partition nodes nodeset (data frame)

objects used for statistics calculation (list with a vector "name", and a vector

"object")

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

startingestimates

first guess for the model parameters

gainfactor numeric used to decrease the size of steps made in the Newton optimization

a.scaling numeric used to reduce the influence of non-diagonal elements in the scaling

matrix (for stability)

r.truncation.p1

numeric used to limit extreme values in the covariance matrix (for stability)

r.truncation.p2

numeric used to limit extreme values in the covariance matrix (for stability)

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

length.p1 number of samples in phase 1

min.iter.p2 minimum number of sub-steps in phase 2 max.iter.p2 maximum number of sub-steps in phase 2

multiplication.iter.p2

value for the lengths of sub-steps in phase 2 (multiplied by 2.52<sup>k</sup>)

 $num.\,steps.\,p2 \qquad number\ of\ optimisation\ steps\ in\ phase\ 2$ 

length.p3 number of samples in phase 3

neighborhood way of choosing partitions: probability vector (actors swap, merge/division, sin-

gle actor move)

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled (now, it only works for vectors like size\_min:size\_max)

estimate\_ERPM 19

double.averaging

option to average the statistics sampled in each sub-step of phase 2

inv.zcov initial value of the inverted covariance matrix (if a phase 3 was run before) to

bypass the phase 1

inv.scaling initial value of the inverted scaling matrix (if a phase 3 was run before) to bypass

the phase 1

parallel whether the phase 1 and 3 should be parallelized

parallel2 whether there should be several phases 2 run in parallel

cpus how many cores can be used

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

A list with the outputs of the three different phases of the algorithm

```
\# define an arbitrary set of n = 6 nodes with attributes, and an arbitrary covariate matrix
nodes <- data.frame(label = c("A", "B", "C", "D", "E", "F"),</pre>
                     gender = c(1,1,2,1,2,2),
                     age = c(20, 22, 25, 30, 30, 31))
friendship <- matrix(c(0, 1, 1, 1, 0, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 0, 0,
                        0, 1, 1, 0, 0, 1,
                        0, 0, 0, 0, 1, 0), 6, 6, TRUE)
# choose the effects to be included (see manual for all effect names)
effects <- list(names = c("num_groups", "same", "diff", "tie"),</pre>
                 objects = c("partition", "gender", "age", "friendship"))
objects <- list()</pre>
objects[[1]] <- list(name = "friendship", object = friendship)</pre>
# define observed partition
partition \leftarrow c(1,1,2,2,2,3)
# estimate
startingestimates <-c(-2,0,0,0)
estimation <- estimate_ERPM(partition,
                              nodes,
                              objects,
                              effects,
                              startingestimates = startingestimates,
                              burnin = 100,
                              thining = 20,
                              length.p1 = 500, # number of samples in phase 1
```

20 estimate\_logL

estimate\_logL

Estimate log likelihood

# **Description**

Function to estimate the log likelihood of a model for an observed partition

## Usage

```
estimate_logL(
  partition,
 nodes,
  effects,
  objects,
  theta,
  theta_0,
 Μ,
  num.steps,
 burnin,
  thining,
  neighborhoods = c(0.7, 0.3, 0),
  numgroups.allowed = NULL,
  numgroups.simulated = NULL,
  sizes.allowed = NULL,
  sizes.simulated = NULL,
  logL_0 = NULL,
 parallel = FALSE,
  cpus = 1,
  verbose = FALSE
)
```

## **Arguments**

```
partition observed partition nodes node set (data frame)
```

estimate\_logL 21

effects	effects/sufficient statistics (list with a vector "names", and a vector "objects")						
objects	objects used for statistics calculation (list with a vector "name", and a vector "object")						
theta	estimated model parameters						
theta_0	model parameters if all other effects than "num-groups" are fixed to $0$ (basic Dirichlet partition model)						
М	number of steps in the path-sampling algorithm						
num.steps	number of samples in each step						
burnin	integer for the number of burn-in steps before sampling						
thining	integer for the number of thining steps between sampling						
neighborhoods	= $c(0.7,0.3,0)$ way of choosing partitions						
numgroups.allo	wed						
	= NULL, # vector containing the number of groups allowed in the partition (now, it only works with vectors like num_min:num_max)						
numgroups.simulated							
	= NULL, # vector containing the number of groups simulated						
sizes.allowed	= NULL, vector of group sizes allowed in sampling (now, it only works for vectors like size_min:size_max)						
sizes.simulate	d						
	= NULL, vector of group sizes allowed in the Markov chain but not necessraily sampled (now, it only works for vectors like size_min:size_max)						
logL_0	= NULL, if known, the value of the log likelihood of the basic dirichlet model						
parallel	= FALSE, indicating whether the code should be run in parallel						
cpus	= 1, number of cpus required for the parallelization						
verbose	= FALSE, to print the current step the algorithm is in						

## Value

List with the log likelihood, AIC, lambda and the draws

```
# choose the effects to be included (see manual for all effect names)
effects <- list(names = c("num_groups","same","diff","tie"),</pre>
objects = c("partition", "gender", "age", "friendship"))
objects <- list()</pre>
objects[[1]] <- list(name = "friendship", object = friendship)</pre>
# define observed partition
partition <- c(1,1,2,2,2,3)
# (an exemplary estimation is internally stored in order to save time)
# first: estimate the ML estimates of a simple model with only one parameter
# for number of groups (this parameter should be in the model!)
likelihood_function <- function(x){ exp(x*max(partition)) / compute_numgroups_denominator(n,x)}
curve(likelihood_function, from=-2, to=0)
parameter_base <- optimize(likelihood_function, interval=c(-2, 0), maximum=TRUE)</pre>
parameters_basemodel <- c(parameter_base$maximum,0,0,0)</pre>
# estimate logL and AIC
logL_AIC <- estimate_logL(partition,</pre>
                           nodes,
                           effects,
                           objects,
                           theta = estimation$results$est,
                           theta_0 = parameters_basemodel,
                           num.steps = 200,
                           burnin = 100,
                           thining = 20)
logL_AIC$logL
logL_AIC$AIC
```

estimate\_multipleERPM Estimate ERPM for multiple observations

#### **Description**

Function to estimate a given model for given observed (multiple) partitions. All options of the algorithm can be specified here.

# Usage

```
estimate_multipleERPM(
  partitions,
  presence.tables,
  nodes,
  objects,
```

```
effects,
      startingestimates,
      gainfactor = 0.1,
      a.scaling = 0.8,
      r.truncation.p1 = -1,
      r.truncation.p2 = -1,
      burnin = 30,
      thining = 10,
      length.p1 = 100,
      min.iter.p2 = NULL,
      max.iter.p2 = NULL,
      multiplication.iter.p2 = 200,
      num.steps.p2 = 6,
      length.p3 = 1000,
      neighborhood = c(0.7, 0.3, 0),
      fixed.estimates = NULL,
      numgroups.allowed = NULL,
      numgroups.simulated = NULL,
      sizes.allowed = NULL,
      sizes.simulated = NULL,
      double.averaging = FALSE,
      inv.zcov = NULL,
      inv.scaling = NULL,
      parallel = FALSE,
      parallel2 = FALSE,
      cpus = 1,
      verbose = FALSE
    )
Arguments
    partitions
                     observed partitions
    presence.tables
                     XXX
    nodes
                     nodeset (data frame)
                     objects used for statistics calculation (list with a vector "name", and a vector
    objects
                     "object")
                     effects/sufficient statistics (list with a vector "names", and a vector "objects")
    effects
    startingestimates
                     first guess for the model parameters
    gainfactor
                     numeric used to decrease the size of steps made in the Newton optimization
    a.scaling
                     numeric used to reduce the influence of non-diagonal elements in the scaling
                     matrix (for stability)
    r.truncation.p1
                     numeric used to limit extreme values in the covariance matrix (for stability)
    r.truncation.p2
                     numeric used to limit extreme values in the covariance matrix (for stability)
```

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

length.p1 number of samples in phase 1

min.iter.p2 minimum number of sub-steps in phase 2 max.iter.p2 maximum number of sub-steps in phase 2

multiplication.iter.p2

value for the lengths of sub-steps in phase 2 (multiplied by 2.52<sup>k</sup>)

num.steps.p2 number of optimisation steps in phase 2

length.p3 number of samples in phase 3

neighborhood way of choosing partitions: probability vector (actors swap, merge/division, sin-

gle actor move)

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num min:num max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size min:size max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

double.averaging

option to average the statistics sampled in each sub-step of phase 2

inv.zcov initial value of the inverted covariance matrix (if a phase 3 was run before) to

bypass the phase 1

inv.scaling initial value of the inverted scaling matrix (if a phase 3 was run before) to bypass

the phase 1

parallel whether the phase 1 and 3 should be parallelized

parallel2 whether there should be several phases 2 run in parallel

cpus how many cores can be used

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

A list with the outputs of the three different phases of the algorithm

estimation

```
\# define an arbitrary set of n = 6 nodes with attributes, and an arbitrary covariate matrix
n <- 6
nodes <- data.frame(label = c("A", "B", "C", "D", "E", "F"),</pre>
                     gender = c(1,1,2,1,2,2),
                     age = c(20, 22, 25, 30, 30, 31)
friendship <- matrix(c(0, 1, 1, 1, 0, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 1, 0,
                        1, 0, 0, 0, 0, 0,
                        0, 1, 1, 0, 0, 1,
                        0, 0, 0, 0, 1, 0), 6, 6, TRUE)
# specify whether nodes are present at different points of time
presence.tables \leftarrow matrix(c(1, 1, 1, 1, 1, 1,
                             0, 1, 1, 1, 1, 1,
                             1, 0, 1, 1, 1, 1), 6, 3)
# choose effects to be included in the estimated model
effects_multiple <- list(names = c("num_groups", "same", "diff", "tie", "inertia_1"),</pre>
                objects = c("partitions", "gender", "age", "friendship", "partitions"),
objects2 = c("", "", "", "", ""))
objects_multiple <- list()</pre>
objects_multiple[[1]] <- list(name = "friendship", object = friendship)</pre>
# define the observation
NA, 1, 1, 2, 2, 2,
                        1, NA, 2, 3, 3, 1), 6, 3)
# estimate
startingestimates <-c(-2,0,0,0,0)
estimation <- estimate_multipleERPM(partitions,</pre>
                                      presence.tables,
                                      nodes,
                                      objects_multiple,
                                      effects_multiple,
                                      startingestimates = startingestimates,
                                      burnin = 100,
                                      thining = 50,
                                      gainfactor = 0.6,
                                      length.p1 = 200,
                                      multiplication.iter.p2 = 20,
                                      num.steps.p2 = 4,
                                      length.p3 = 1000)
# get results table
```

26 find\_all\_partitions

```
exactestimates_numgroups
```

Exact estimates number of groups

# Description

This function finds the best estimate for a model only including the statistics of number of groups. It does a grid search for a vector of potential parameters, for all numbers of groups.

## Usage

```
exactestimates_numgroups(num.nodes, pmin, pmax, pinc)
```

## **Arguments**

num.nodesnumber of nodespminlowest parameter valuepmaxhighest parameter value

pinc increment between different parameter values

## Value

a list

find\_all\_partitions

Function to enumerate all possible partitions for a given n

## **Description**

Function to enumerate all possible partitions for a given n

#### Usage

```
find_all_partitions(n)
```

# Arguments

n

number of nodes

# Value

matrix where each line corresponds to a possible partition

```
n <- 6
all_partitions <- find_all_partitions(n)</pre>
```

```
\label{eq:continuous_multiple} \textit{Grid - search burnin thining multiple}
```

## **Description**

Function that simulates the Markov chain for a given model and several sets of transitions (the neighborhoods), for multiple partitions. For each neighborhood, it calculates the autocorrelation of statistics for different thinings and the average statistics for different burn-ins. Then the best neighborhood can be selected along with good values for burn-in and thining

# Usage

```
gridsearch_burninthining_multiple(
 partitions,
 presence.tables,
  theta,
  nodes,
 effects,
 objects,
  num.steps,
  neighborhoods,
 numgroups.allowed,
 numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
 max.thining,
 parallel = FALSE,
  cpus = 1
)
```

# Arguments

partitions Observed partitions							
presence.tables	presence.tables						
	Presence of nodes						
theta	Initial model parameters						
nodes	Node set (data frame)						
effects	Effects/sufficient statistics (list with a vector "names", and a vector "objects")						
objects	Objects used for statistics calculation (list with a vector "name", and a vector "object")						
num.steps	Number of samples wanted						
neighborhoods	List of probability vectors (proba actors swap, proba merge/division, proba single actor move) $$						

```
numgroups.allowed
```

vector containing the number of groups allowed in the partition (now, it only works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

max.thining Where to stop adding thining

parallel False, to run different neighborhoods in parallel

cpus Equal to 1

#### Value

list

```
gridsearch_burninthining_single
```

Grid - search burnin thining single

#### **Description**

Function that simulates the Markov chain for a given model and several sets of transitions (the neighborhoods), for a single partition. For each neighborhood, it calculates the autocorrelation of statistics for different thinings and the average statistics for different burn-ins. Then the best neighborhood can be selected along with good values for burn-in and thining

#### Usage

```
gridsearch_burninthining_single(
  partition,
  theta,
  nodes,
  effects,
  objects,
  num.steps,
  neighborhoods,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
 max.thining,
 parallel = FALSE,
  cpus = 1
)
```

#### **Arguments**

partition A partition (vector)
theta Initial model parameters

nodes Node set (data frame)

effects Effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects Used for statistics calculation (list with a vector "name", and a vector

"object")

num.steps Number of samples wanted

neighborhoods List of probability vectors (proba actors swap, proba merge/division, proba sin-

gle actor move)

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

max.thining Where to stop adding thining

parallel False, to run different neighborhoods in parallel

cpus Equal to 1

#### Value

list

gridsearch\_burnin\_single

Grid - search burnin single

## **Description**

Function that can be used to find a good length for the burn-in of the Markov chain for a given model and differents sets of transitions in the chain (the neighborhoods). For each neighborhood, it draws a chain and calculates the mean statistics for different burn-ins.

#### Usage

```
gridsearch_burnin_single(
  partition,
  theta,
  nodes,
  effects,
  objects,
  num.steps,
  neighborhoods,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  parallel = FALSE,
  cpus = 1
)
```

A partition (vector)

#### **Arguments**

partition

theta Initial model parameters nodes Node set (data frame) effects Effects/sufficient statistics (list with a vector "names", and a vector "objects") Objects used for statistics calculation (list with a vector "name", and a vector objects "object") num.steps Number of samples wanted neighborhoods List of probability vectors (proba actors swap, proba merge/division, proba single actor move) numgroups.allowed = NULL, # vector containing the number of groups allowed in the partition (now, it only works with vectors like num\_min:num\_max) numgroups.simulated vector containing the number of groups simulated sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like size\_min:size\_max)

(now, it only works for vectors like size\_min:size\_max)

False, to run different neighborhoods in parallel

Vector of group sizes allowed in the Markov chain but not necessraily sampled

#### Value

all simulations

parallel

cpus

sizes.simulated

Equal to 1

```
gridsearch_thining_single

Grid - search thining single
```

## **Description**

Function that can be used to find a good length for the thining of the Markov chain for a given model and differents sets of transitions in the chain (the neighborhoods). For each neighborhood, it draws a chain and calculates the autocorrelation of statistics for different thinings.

## Usage

```
gridsearch_thining_single(
  partition,
  theta,
  nodes,
  effects,
  objects,
  num.steps,
  neighborhoods,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  burnin,
  max.thining,
  parallel = FALSE,
  cpus = 1
)
```

# Arguments

```
partition
                  A partition (vector)
theta
                  Initial model parameters
nodes
                  Node set (data frame)
                  Effects/sufficient statistics (list with a vector "names", and a vector "objects")
effects
                  Objects used for statistics calculation (list with a vector "name", and a vector
objects
                  "object")
num.steps
                  Number of samples wanted
neighborhoods
                  List of probability vectors (proba actors swap, proba merge/division, proba sin-
                  gle actor move)
numgroups.allowed
                  vector containing the number of groups allowed in the partition (now, it only
                  works with vectors like num_min:num_max)
```

32 group\_size

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

burnin length of the burn-in period

max.thining maximal value for the thining to be tested

parallel False, to run different neighborhoods in parallel

cpus Equal to 1

#### Value

all simulations

group\_size

Statistics on the size of groups in a partition

# Description

This function computes the average or the standard deviation of the size of groups in a partition.

## Usage

```
group_size(partition, stat)
```

#### **Arguments**

partition A partition (vector)

stat The statistic to compute: 'avg' for average and 'sd' for standard deviation

## Value

A number corresponding to the correlation coefficient if the attribute is numerical or the correlation ratio if the attribute is categorical.

```
p <- c(1,2,2,3,3,4,4,4,5)
group_size(p,'avg')
group_size(p,'sd')</pre>
```

icc 33

icc Intra class correlation

# Description

This function computes the intra class correlation correlation of attributes for 2 randomly drawn individuals in the same group.

## Usage

```
icc(partition, attribute)
```

#### **Arguments**

partition A partition

attribute A vector containing the values of the attribute

## Value

A number corresponding to the ICC

## **Examples**

```
p \leftarrow c(1,2,2,3,3,4,4,4,5)
at \leftarrow c(3,5,23,2,1,0,3,9,2)
icc(p, at)
```

number\_categories

Number of individuals having an attribute

# Description

This function computes the total number of individuals being in a category of an attribute in a partition. It also computes the sum of the proportion in each group of individuals being in a category.

#### Usage

```
number_categories(partition, attribute, stat, category)
```

# Arguments

partition	A partition (vector)
attribute	A vector containing the values of the attribute
stat	The statistic to compute: 'avg' for the sum of proportion per group and 'sum' for the total number
category	The category to consider or category = 'all' if all categories have to be considered

number\_ties

## Value

The statistic chosen in stat depending on the value of category. If category = 'all', returns a vector.

#### **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(1,0,0,0,1,1,0,0,1)
number_categories(p,at,'avg','all')</pre>
```

number\_ties

Same pairs of individuals in a partition

# Description

This function computes the number of ties.

#### Usage

```
number_ties(partition, dyadic_attribute, stat)
```

# Arguments

```
\label{eq:partition} \text{Partition (vector)} \\ \text{dyadic\_attribute}
```

A matrix containing the values of the attribute

stat

The statistic to compute: 'avg\_pergroup' for the average per group, 'sum\_pergroup' for the sum, 'sum\_perind' and 'avg\_perind' for the number of ties per individuals each individual has in its group.

#### Value

The statisic chosen in stat

order\_groupids 35

order_groupids	Function to replace the ids of the group without forgetting an id and put in the first appearance order for example: [2 1 1 4 2] becomes [1 2 2 3 1]

# Description

Function to replace the ids of the group without forgetting an id and put in the first appearance order for example: [2 1 1 4 2] becomes [1 2 2 3 1]

# Usage

```
order_groupids(partition)
```

## **Arguments**

partition observed partition

## Value

a vector (partition)

outcomeObjects

Exemplary outcome objects for the ERPM Package

# Description

These are exemplary outcome objects for the ERPM package and can be used in order not to run all precedent functions and thus save time. The following products are provided:

# **Format**

estimation An results object created by the function estimate\_ERPM().

phase1

phase1

Core function for Phase 1

#### Description

Core function for Phase 1

#### Usage

```
phase1(
    startingestimates,
    inv.zcov,
    inv.scaling,
    z.phase1,
    z.obs,
    nodes,
    effects,
    objects,
    r.truncation.p1,
    length.p1,
    fixed.estimates,
    verbose = FALSE
)
```

#### **Arguments**

startingestimates

vector containing initial parameter values

inv.zcov inverted covariance matrix

inv.scaling scaling matrix

z.phase1 statistics retrieved from phase 1

z.obs observed statistics nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")
objects objects used for statistics calculation (list with a vector "name", and a vector

"object")

r.truncation.p1

numeric used to limit extreme values in the covariance matrix (for stability)

length.p1 number of samples in phase 1

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

plot\_averagesizes 37

#### Value

estimated parameters after phase 1

plot\_averagesizes

Plot average sizes

## **Description**

Function to plot the average size of a random partition depending on the number of nodes

## Usage

```
plot_averagesizes(nmin, nmax, ninc)
```

## **Arguments**

nmin minimum number of nodes nmax maximum number of nodes

ninc increment between the different number of nodes

#### Value

a vector

```
plot_numgroups_likelihood
```

Plot likelihood of number groups

# Description

Function to plot the log-likelihood of the model with a single statistic (number of groups) depending on the parameter value for this statistic

#### Usage

```
plot_numgroups_likelihood(m.obs, num.nodes, pmin, pmax, pinc)
```

## **Arguments**

m. obs observed number of groups

num.nodes number of nodes

pmin lowest parameter value pmax highest parameter value

pinc increment between different parameter values

38 plot\_partition

#### Value

a vector

plot\_partition

Visualization of partition

# Description

This function plot the groups of a partition

# Usage

```
plot_partition(
  partition,
  title = NULL,
  group.color = NULL,
  attribute.color = NULL,
  attribute.shape = NULL
)
```

## Arguments

#### Value

A plot of the partition

# **Examples**

```
\begin{array}{lll} p <- & c(1,1,1,2,2,2,2,3,3,3,4,4,4,4,4) \\ attr1 <- & c(1,0,0,1,0,0,1,0,1,0,1,1,1,1,1,2) \\ attr2 <- & c(1,1,1,1,0,0,3,0,1,0,1,1,1,1,1,2) \\ plot_partition(p,attribute.color = attr1, attribute.shape = attr2) \end{array}
```

```
print.results.bayesian.erpm
```

Print results of bayesian estimation (beta version)

# Description

Print results of bayesian estimation (beta version)

## Usage

```
## S3 method for class 'results.bayesian.erpm' print(x, ...)
```

# Arguments

x output of the bayesian estimate function

... For internal use only.

#### Value

a data frame

```
print.results.list.erpm
```

Print estimation results

# Description

Print estimation results

# Usage

```
## S3 method for class 'results.list.erpm'
print(x, ...)
```

# Arguments

x output of the estimate function

... For internal use only.

#### Value

a data frame

40 proportion\_isolate

```
print.results.p3.erpm Print results of estimation of phase 3
```

## **Description**

Print results of estimation of phase 3

# Usage

```
## S3 method for class 'results.p3.erpm'
print(x, ...)
```

# Arguments

x output of the estimate function

... For internal use only.

#### Value

a data frame

```
proportion_isolate
```

Proportion of isolates

# Description

This function computes the proportion of individuals not joining others.

# Usage

```
proportion_isolate(partition)
```

# Arguments

```
partition A
```

A partition (vector)

#### Value

A number corresponding to proportion of individuals alone.

## **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
proportion_isolate(p)</pre>
```

range\_attribute 41

|--|

# Description

This function computes the sum or the average range of an attribute for groups in a partition.

# Usage

```
range_attribute(partition, attribute, stat)
```

# Arguments

partition A partition (vector)

attribute A vector containing the values of the attribute

stat The statistic to compute: 'avg\_pergroup' for the average per group and 'sum\_pergroup'

for the sum of the ranges

#### Value

The statisic chosen in stat

## **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(3,5,23,2,1,0,3,9,2)
range_attribute(p,at,'avg_pergroup')</pre>
```

run\_phase1\_multiple

Phase 1 wrapper for multiple observations

# Description

Phase 1 wrapper for multiple observations

```
run_phase1_multiple(
  partitions,
  startingestimates,
  z.obs,
  presence.tables,
  nodes,
  effects,
  objects,
```

```
burnin,
      thining,
      gainfactor,
      a.scaling,
      r.truncation.p1,
      length.p1,
      neighborhood,
      fixed.estimates,
      numgroups.allowed,
      numgroups.simulated,
      sizes.allowed,
      sizes.simulated,
      parallel = FALSE,
      cpus = 1,
      verbose = FALSE
    )
Arguments
    partitions
                      observed partitions
    startingestimates
                      vector containing initial parameter values
                      observed statistics
    z.obs
    presence.tables
                      data frame to indicate which times nodes are present in the partition
                      node set (data frame)
    nodes
    effects
                      effects/sufficient statistics (list with a vector "names", and a vector "objects")
                      objects used for statistics calculation (list with a vector "name", and a vector
    objects
                      "object")
    burnin
                      integer for the number of burn-in steps before sampling
    thining
                      integer for the number of thining steps between sampling
    gainfactor
                      gain factor (useless now)
    a.scaling
                      scaling factor
    r.truncation.p1
                      truncation factor (for stability)
    length.p1
                      number of samples for phase 1
    neighborhood
                      vector for the probability of choosing a particular transition in the chain
    fixed.estimates
                      if some parameters are fixed, list with as many elements as effects, these ele-
                      ments equal a fixed value if needed, or NULL if they should be estimated
    numgroups.allowed
                      vector containing the number of groups allowed in the partition (now, it only
                      works with vectors like num_min:num_max)
    numgroups.simulated
```

vector containing the number of groups simulated

43 run\_phase1\_single

vector of group sizes allowed in sampling (now, it only works for vectors like sizes.allowed size\_min:size\_max) sizes.simulated vector of group sizes allowed in the Markov chain but not necessarily sampled (now, it only works for vectors like size\_min:size\_max) parallel boolean to indicate whether the code should be run in parallel cpus number of cpus if parallel = TRUE

logical: should intermediate results during the estimation be printed or not?

verbose

Defaults to FALSE.

#### Value

a list

run\_phase1\_single

Phase 1 wrapper for single observation

## **Description**

Phase 1 wrapper for single observation

```
run_phase1_single(
  partition,
  startingestimates,
 z.obs,
 nodes,
 effects,
 objects,
 burnin,
  thining,
  gainfactor,
  a.scaling,
  r.truncation.p1,
  length.p1,
  neighborhood,
  fixed.estimates,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
 parallel = TRUE,
 cpus = 1,
  verbose = FALSE
)
```

44 run\_phase1\_single

#### **Arguments**

partition observed partition

startingestimates

vector containing initial parameter values

z.obs observed statistics nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects objects used for statistics calculation (list with a vector "name", and a vector

"object")

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

gainfactor gain factor (useless now)

a.scaling scaling factor

r.truncation.p1

truncation factor (for stability)

length.p1 number of samples for phase 1

neighborhood vector for the probability of choosing a particular transition in the chain

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size min:size max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessarily sampled

(now, it only works for vectors like size\_min:size\_max)

parallel boolean to indicate whether the code should be run in parallel

cpus number of cpus if parallel = TRUE

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

## Value

a list

run\_phase2\_multiple

45

run\_phase2\_multiple

Phase 2 wrapper for multiple observation

## **Description**

Phase 2 wrapper for multiple observation

## Usage

```
run_phase2_multiple(
  partitions,
 estimates.phase1,
  inv.zcov,
  inv.scaling,
  z.obs,
 presence.tables,
 nodes,
 effects,
  objects,
  burnin,
  thining,
  num.steps,
 gainfactors,
  r.truncation.p2,
 min.iter,
 max.iter,
 multiplication.iter,
 neighborhood,
  fixed.estimates,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  double.averaging,
  parallel = FALSE,
  cpus = 1,
  verbose = FALSE
)
```

```
partitions observed partitions
estimates.phase1
vector containing parameter values after phase 1
inv.zcov inverted covariance matrix
inv.scaling scaling matrix
```

z.obs observed statistics

presence.tables

data frame to indicate which times nodes are present in the partition

nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects objects used for statistics calculation (list with a vector "name", and a vector

"object")

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

num. steps number of sub-phases in phase 2

gainfactors vector of gain factors

r.truncation.p2

truncation factor

min.iter minimum numbers of steps in each subphase max.iter maximum numbers of steps in each subphase

multiplication.iter

used to calculate min.iter and max.iter if not specified

neighborhood vector for the probability of choosing a particular transition in the chain

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

double.averaging

boolean to indicate whether we follow the double-averaging procedure (often

leads to better convergence)

parallel boolean to indicate whether the code should be run in parallel

cpus number of cpus if parallel = TRUE

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

a list

run\_phase2\_single 47

run\_phase2\_single

Phase 2 wrapper for single observation

## **Description**

Phase 2 wrapper for single observation

# Usage

```
run_phase2_single(
  partition,
 estimates.phase1,
  inv.zcov,
  inv.scaling,
  z.obs,
 nodes,
 effects,
 objects,
 burnin,
  thining,
  num.steps,
 gainfactors,
  r.truncation.p2,
 min.iter,
 max.iter,
 multiplication.iter,
 neighborhood,
  fixed.estimates,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  double.averaging,
  parallel = FALSE,
 cpus = 1,
  verbose = FALSE
)
```

```
partition observed partition
estimates.phase1
vector containing parameter values after phase 1
inv.zcov inverted covariance matrix
inv.scaling scaling matrix
z.obs observed statistics
```

48 run\_phase2\_single

nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects used for statistics calculation (list with a vector "name", and a vector

"object")

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

num.steps number of sub-phases in phase 2

gainfactors vector of gain factors

r.truncation.p2

truncation factor

min.iter minimum numbers of steps in each subphase max.iter maximum numbers of steps in each subphase

multiplication.iter

used to calculate min.iter and max.iter if not specified

neighborhood vector for the probability of choosing a particular transition in the chain

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only works with vectors like num min:num max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

double.averaging

boolean to indicate whether we follow the double-averaging procedure (often

leads to better convergence)

parallel boolean to indicate whether the code should be run in parallel

cpus number of cpus if parallel = TRUE

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

a list

run\_phase3\_multiple 49

run\_phase3\_multiple Phase 3 wrapper for multiple observation

## **Description**

Phase 3 wrapper for multiple observation

# Usage

```
run_phase3_multiple(
  partitions,
 estimates.phase2,
 z.obs,
  presence.tables,
 nodes,
 effects,
 objects,
  burnin,
  thining,
  a.scaling,
  length.p3,
  neighborhood,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  fixed.estimates,
 parallel = FALSE,
  cpus = 1,
  verbose = FALSE
)
```

```
partitions
                   observed partitions
estimates.phase2
                   vector containing parameter values after phase 2
z.obs
                   observed statistics
presence.tables
                   data frame to indicate which times nodes are present in the partition
nodes
                  node set (data frame)
effects
                   effects/sufficient statistics (list with a vector "names", and a vector "objects")
objects
                   objects used for statistics calculation (list with a vector "name", and a vector
                   "object")
burnin
                  integer for the number of burn-in steps before sampling
```

50 run\_phase3\_single

thining integer for the number of thining steps between sampling

a. scaling multiplicative factor for out-of-diagonal elements of the covariance matrix

length.p3 number of samples in phase 3

neighborhood vector for the probability of choosing a particular transition in the chain

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these ele-

ments equal a fixed value if needed, or NULL if they should be estimated

parallel boolean to indicate whether the code should be run in parallel

cpus number of cpus if parallel = TRUE

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

a list

run\_phase3\_single

Phase 3 wrapper for single observation

## **Description**

Phase 3 wrapper for single observation

```
run_phase3_single(
  partition,
  estimates.phase2,
  z.obs,
  nodes,
  effects,
  objects,
  burnin,
  thining,
```

run\_phase3\_single 51

```
a.scaling,
length.p3,
neighborhood,
numgroups.allowed,
numgroups.simulated,
sizes.allowed,
sizes.simulated,
fixed.estimates,
parallel = FALSE,
cpus = 1,
verbose = FALSE
```

## **Arguments**

partition observed partition

estimates.phase2

vector containing parameter values after phase 2

z.obs observed statistics nodes node set (data frame)

effects effects/sufficient statistics (list with a vector "names", and a vector "objects")
objects objects used for statistics calculation (list with a vector "name", and a vector

"object")

burnin integer for the number of burn-in steps before sampling thining integer for the number of thining steps between sampling

a.scaling multiplicative factor for out-of-diagonal elements of the covariance matrix

length.p3 number of sampled partitions in phase 3

neighborhood vector for the probability of choosing a particular transition in the chain

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

fixed.estimates

if some parameters are fixed, list with as many elements as effects, these elements equal a fixed value if needed, or NULL if they should be estimated

parallel boolean to indicate whether the code should be run in parallel

cpus number of cpus if parallel = TRUE

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

52 similar\_pairs

#### Value

a list

same\_pairs

Same pairs of individuals in a partition

## **Description**

This function computes the total number, the average number having the same value of a categorical variable and the number of individuals a partition.

# Usage

```
same_pairs(partition, attribute, stat)
```

## **Arguments**

partition A partition (vector)

attribute A vector containing the values of the attribute

stat The statistic to compute: 'avg\_pergroup' for the average, 'sum\_pergroup' for

the sum, 'sum\_perind' and 'avg\_perind' for the number of ties per individual

each individual has in its group.

#### Value

The statistic chosen in stat

## **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(0,1,1,1,1,0,0,0,0)
same_pairs(p,at,'avg_pergroup')</pre>
```

similar\_pairs

Similar pairs of individuals in a partition

## Description

This function computes the total number, the average number having the close values of a numerical variable and the number of individuals a partition.

```
similar_pairs(partition, attribute, stat, threshold)
```

#### **Arguments**

partition A partition (vector)

attribute A vector containing the values of the attribute

stat The statistic to compute: 'avg\_pergroup' for the average, 'sum\_pergroup' for

the sum, 'sum\_perind' and 'avg\_perind' for individuals

threshold Threshold to determine if 2 individuals attributes values are close

#### Value

The statisic chosen in stat

## **Examples**

```
p <- c(1,2,2,3,3,4,4,4,5)
at <- c(3,5,23,2,1,0,3,9,2)
similar_pairs(p,at,1,'avg_pergroup')</pre>
```

```
simulate_burninthining_multiple
```

Simulate burnin thining multiple

# **Description**

Function that simulates the Markov chain for a given model and a set of transitions (the neighborhood), for multiple partitions. It calculates the autocorrelation of statistics for different thinings and the average statistics for different burn-ins.

```
simulate_burninthining_multiple(
 partitions,
 presence.tables,
  theta,
 nodes,
 effects,
  objects,
  num.steps,
  neighborhood,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
 max.thining,
  verbose = FALSE
)
```

#### **Arguments**

partitions Observed partitions

presence.tables

to indicate which nodes were present when

theta Initial model parameters nodes Node set (data frame)

effects Effects/sufficient statistics (list with a vector "names", and a vector "objects")

"object")

num. steps Number of samples wanted

neighborhood Way of choosing partitions: probability vector (proba actors swap, proba merge/division,

proba single actor move)

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

max.thining maximal number of simulated steps in the thining

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

A list

simulate\_burninthining\_single

Simulate burnin thining single

## **Description**

Function that simulates the Markov chain for a given model and a set of transitions (the neighborhood), for a single partition. It calculates the autocorrelation of statistics for different thinings and the average statistics for different burn-ins.

## **Usage**

```
simulate_burninthining_single(
  partition,
  theta,
  nodes,
  effects,
  objects,
  num.steps,
  neighborhood,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
  max.thining,
  verbose = FALSE
)
```

## **Arguments**

partition Observed partition (vector)
theta Initial model parameters
nodes Node set (data frame)
effects Effects/sufficient statistics (

effects Effects/sufficient statistics (list with a vector "names", and a vector "objects")

objects used for statistics calculation (list with a vector "name", and a vector

"object")

num. steps Number of samples wanted

neighborhood Way of choosing partitions: probability vector (proba actors swap, proba merge/division,

proba single actor move)

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

max. thining maximal number of simulated steps in the thining

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

A list

```
simulate_burnin_single
```

Simulate burn in single

# Description

Function that can be used to find a good length for the burn-in of the Markov chain for a given model and a given set of transitions in the chain (the neighborhood). It draws a chain and calculates the mean statistics for different burn-ins.

# Usage

```
simulate_burnin_single(
  partition,
  theta,
  nodes,
  effects,
  objects,
  num.steps,
  neighborhood,
  numgroups.allowed,
  numgroups.simulated,
  sizes.allowed,
  sizes.simulated
)
```

partition	A partition (vector)		
theta	Initial model parameters		
nodes	Node set (data frame)		
effects	Effects/sufficient statistics (list with a vector "names", and a vector "objects")		
objects	Objects used for statistics calculation (list with a vector "name", and a vector "object")		
num.steps	Number of samples wanted		
neighborhood	Way of choosing partitions: probability vector (proba actors swap, proba merge/division, proba single actor move)		
numgroups.allowed			
	vector containing the number of groups allowed in the partition (now, it only works with vectors like num_min:num_max)		
numgroups.simulated			
	vector containing the number of groups simulated		
sizes.allowed	Vector of group sizes allowed in sampling (now, it only works for vectors like size_min:size_max)		

```
sizes.simulated
```

Vector of group sizes allowed in the Markov chain but not necessraily sampled (now, it only works for vectors like size\_min:size\_max)

#### Value

A list with list the draws, the moving means and the moving means smoothed

## **Description**

Function that can be used to find a good length for the thining of the Markov chain for a given model and a set of transitions in the chain (the neighborhood). It draws a chain and calculates the autocorrelation of statistics for different thinings.

## Usage

```
simulate_thining_single(
  partition,
  theta,
 nodes,
 effects,
 objects,
  num.steps,
 neighborhood,
 numgroups.allowed,
 numgroups.simulated,
  sizes.allowed,
  sizes.simulated,
 burnin,
 max.thining,
  verbose = FALSE
)
```

partition	A partition (vector)
theta	Initial model parameters
nodes	Node set (data frame)
effects	Effects/sufficient statistics (list with a vector "names", and a vector "objects")
objects	Objects used for statistics calculation (list with a vector "name", and a vector "object")
num.steps	Number of samples wanted

58 Stirling2\_constraints

neighborhood Way of choosing partitions: probability vector (proba actors swap, proba merge/division,

proba single actor move)

numgroups.allowed

vector containing the number of groups allowed in the partition (now, it only

works with vectors like num\_min:num\_max)

numgroups.simulated

vector containing the number of groups simulated

sizes.allowed Vector of group sizes allowed in sampling (now, it only works for vectors like

size\_min:size\_max)

sizes.simulated

Vector of group sizes allowed in the Markov chain but not necessraily sampled

(now, it only works for vectors like size\_min:size\_max)

burnin number of simulated steps for the burn-in

max.thining maximal number of simulated steps in the thining

verbose logical: should intermediate results during the estimation be printed or not?

Defaults to FALSE.

#### Value

A list

Stirling2\_constraints Function to calculate the number of partitions with k groups of sizes between smin and smax

# **Description**

Function to calculate the number of partitions with k groups of sizes between smin and smax

## Usage

```
Stirling2_constraints(n, k, smin, smax)
```

## **Arguments**

n number of nodes k number of groups

smin minimum group size possible in the partition smax maximum group size possible in the partition

#### Value

a numeric

Stirling2\_constraints 59

# Examples

```
n <- 6
k <- 2
size_min <- 2
size_max <- 4
Stirling2_constraints(n,k,size_min,size_max)</pre>
```

# **Index**

* datasets	number_ties, 34
outcomeObjects, 35	
	order_groupids,35
Bell_constraints, 3	outcomeObjects, 35
${\tt calculate\_denominator\_Dirichlet\_restricted},$	phase1, 36
4	plot_averagesizes, 37
<pre>calculate_proba_Dirichlet_restricted,     4</pre>	plot_numgroups_likelihood, 37 plot_partition, 38
check_sizes, 5	print.results.bayesian.erpm, 39
compute_averagesize, 7	print.results.list.erpm, 39
compute_numgroups_denominator, 8	print.results.p3.erpm, 40
computeStatistics, 6	proportion_isolate, 40
computeStatistics_multiple, 6	
correlation_between, 8	range_attribute,41
correlation_with_size, 10	<pre>run_phase1_multiple, 41</pre>
correlation_within, 9	run_phase1_single,43
count_classes, 10	<pre>run_phase2_multiple, 45</pre>
CUP, 11	run_phase2_single,47
	run_phase3_multiple,49
draw_Metropolis_multiple, 12	run_phase3_single,50
draw_Metropolis_single, 14	
	same_pairs, 52
estimate_ERPM, 17	similar_pairs, 52
estimate_ERPM(), 35	simulate_burnin_single, 56
estimate_logL, 20	simulate_burninthining_multiple, 53
estimate_multipleERPM, 22	simulate_burninthining_single, 54
estimation (outcomeObjects), 35	simulate_thining_single, 57
exactestimates_numgroups, 26	Stirling2_constraints, 58
${\tt find\_all\_partitions}, 26$	
gridsearch_burnin_single, 29	
<pre>gridsearch_burninthining_multiple, 27</pre>	
<pre>gridsearch_burninthining_single, 28</pre>	
<pre>gridsearch_thining_single, 31</pre>	
group_size, 32	
icc, 33	
number_categories, 33	